## Illustrative Mathematics

## 8.SP.4 Music and Sports (has both reviews)

## Alignment 1: 8.SP.A. 4

Is there an association between whether a student plays a sport and whether he or she plays a musical instrument? To investigate these questions, each student in your class should answer the following two questions:

1. Do you play a sport? (yes or no)
2. Do you play a musical instrument? (yes or no)

Record the answers in the table below.

| Student | Sport? | Musical Instrument? |
| :--- | :--- | :--- |
| 1 |  |  |
| 2 |  |  |
| 3 |  |  |
| 4 |  |  |
| 5 |  |  |
| 6 |  |  |
| 7 |  |  |
| 8 |  |  |
| 9 |  |  |
| 10 |  |  |
| 11 |  |  |
| 12 |  |  |
| 13 |  |  |
| 14 |  |  |
| 15 |  |  |
| 16 |  |  |
| 17 |  |  |
| 18 |  |  |
| 19 |  |  |
| 20 |  |  |
| 21 |  |  |
| 22 |  |  |
| 24 |  |  |

a. Summarize the data into a clearly labeled table.
b. Of those students who play a sport, what proportion play a musical instrument?
c. Of those students who do not play a sport, what proportion play a musical instrument?
d. Based on the class data, do you think there is an association between playing a sport and playing an instrument?
e. Create a graph that would help visualize the association, if any, between playing a sport and playing a musical instrument.

## Commentary:

- Vocal training maybe considered "playing a musical instrument."
- The most commonly used graph to display the relationship between two categorical variables is a segmented bar graph. For segmented bar graphs, we have the categories of the explanatory variable along the $x$-axis (i.e. horizontal axis), with a bar worth $100 \%$ at each category. Each bar is split into segments representing the categories of the response variable. The size of each segment is proportional to the conditional proportions of the categories of the response variable, within each category of the explanatory variable.


## Solution: Solution

Solutions will vary depending on the actual data values collected by the class. Below is a solution based on the following hypothetical data set:

| Student | Sport? | Musical Instrument? |
| :--- | :--- | :--- |
| 1 | Yes | No |
| 2 | Yes | No |
| 3 | Yes | No |
| 4 | No | No |
| 5 | No | Yes |
| 6 | Yes | Yes |
| 7 | No | Yes |
| 8 | Yes | No |
| 9 | No | Yes |
| 10 | Yes | Yes |
| 11 | Yes | No |
| 12 | Yes | Yes |
| 13 | Yes | No |
| 14 | No | No |
| 15 | No | Yes |
| 16 | Yes | Yes |
| 17 | Yes | No |
| 18 | Yes | No |
| 19 | No | Yes |
| 20 | Yes | Yes |
| 21 | Yes | Yes |
| 22 | No | Yes |
| 23 | No | No |
| 24 | No | Yes |

a. The data can be summarized into a two-way table:

|  |  | Sports? |  |  |
| :--- | :--- | :--- | :--- | :--- |
|  |  | Yes | No | Total |
| Musical Instrument? | Yes | 6 | 7 | 13 |
|  | No | 8 | 3 | 11 |
|  | Total | 14 | 10 | 24 |

b. Of those students who play a sport, the proportion who play a musical instrument $=\frac{6}{14}=0.43$
c. Of those students who do not play a sport, the proportion who play a musical instrument $=\frac{7}{10}=0.70$
d. Based on the above data, it appears that students who don't play a sport, are more likely to play a musical instrument
compared to students who do play a sport, as can be seen from the answers to (b) and (c).
e. Here is a segmented bar chart for the above data:

## Playing a sport vs. playing a musical instrument



As can be seen from the above graph, of all those students who reported not playing a sport, $70 \%$ reported playing a musical instrument, whereas $30 \%$ reported not playing a musical instrument. On the other hand, of all those students who reported playing a sport, about $43 \%$ reported playing a musical instrument, compared to $57 \%$ reported not playing a musical instrument.

